

# Higgs Spin / Mixture Overview

Andrei Gritsan (JHU & CMS/LPC)

for

Sally Dawson (BNL), Heather Logan (Carleton),  
Rick Van Kooten (Indiana), Jianming Qian (Michigan),  
Chris Tully (Princeton)

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Higgs Boson Study Group  
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# From the Princeton workshop and the next steps

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- Higgs Snowmass Workshop, 14–15 January 2013, Princeton  
<http://physics.princeton.edu/indico/internalPage.py?pageId=1&confId=127>
- Session on Spin and CP Mixtures
  - Theory overview (Kirill Melnikov)
  - CMS view (Seth Zenz)
  - ATLAS view (Kirill Prokofiev)
  - Lepton / photon colliders: pending contributions (see today)
- Discussed main ideas for Snowmass studies
  - ATLAS+CMS+ have provided good framework for projections
  - Lepton / photon colliders: were seeking active projections
- Next important milestone: have preliminary studies ready by June 15

# Two main paths: spin and mixture

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- Two main paths to study “H(125)”

(1) test of exotic **spin**  $> 0$  assignments / hypothesis testing

LHC is excluding already  $\Rightarrow$  interest may be reducing  
nonetheless, identify **benchmark models** for comparison

(2) measure **mixture**: tensor structure of interactions (spin-0)  
equivalent **effective Lagrangian** or **scattering amplitude** approaches

(2a)  $ZZH$ ,  $WWH$  (SM  **$g_1$** ),  $Z\gamma H$ ,  $\gamma\gamma H$ ,  $ggH$  (SM  **$g_2$** ), or  $0^-$  ( **$g_4$** )

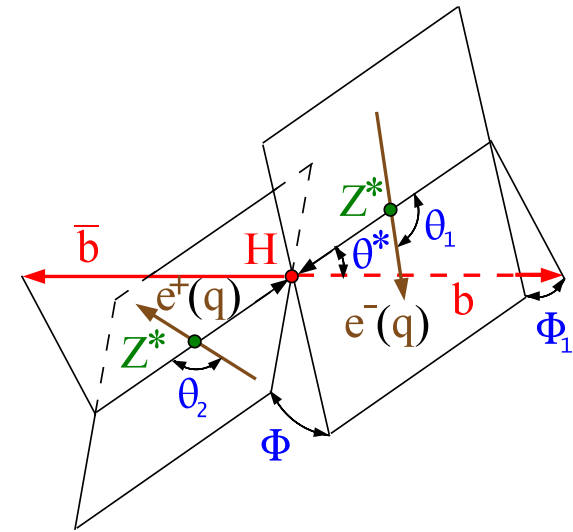
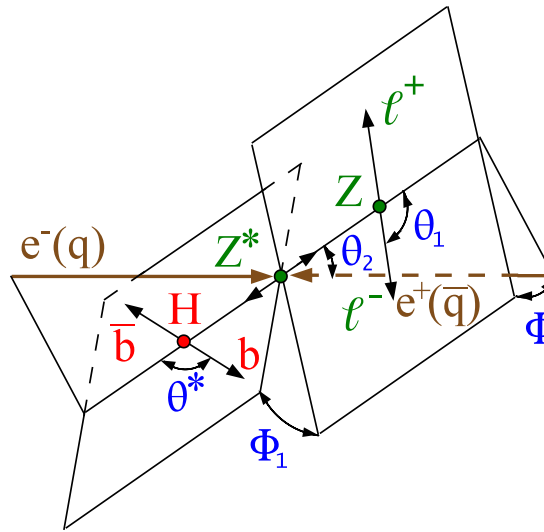
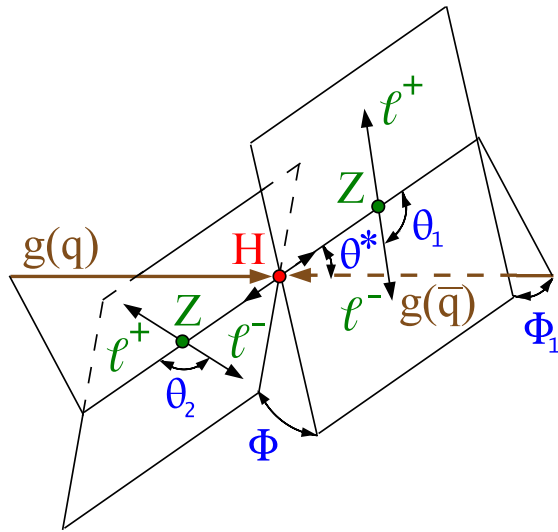
$$A_{VV} \propto \mathbf{g}_1 m_V^2 \epsilon_1^* \epsilon_2^* + \mathbf{g}_2 f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + g_3 f^{*(1),\mu\nu} f_{\mu\alpha}^{*(2)} \frac{q_\nu q^\alpha}{\Lambda^2} + \mathbf{g}_4 f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}$$

$$(2b) \tau^+ \tau^- H, \mu^+ \mu^- H, b\bar{b}H, t\bar{t}H, .. \quad A_{f\bar{f}} \propto \frac{m_f}{v} \bar{u}_2 (\mathbf{\rho}_1 + \mathbf{\rho}_2 \gamma_5) v_1$$

$$(\text{field strength tensor } V^{\mu\nu} \Leftrightarrow f^{(i),\mu\nu} = \epsilon_i^\mu q_i^\nu - \epsilon_i^\nu q_i^\mu)$$

# “Golden” comparison: $pp$ vs $e^+e^-$

- LHC:  $gg \rightarrow H$
- H-factory:  $ee \rightarrow ZH$
- ILC:  $eeZZ \rightarrow eeH$



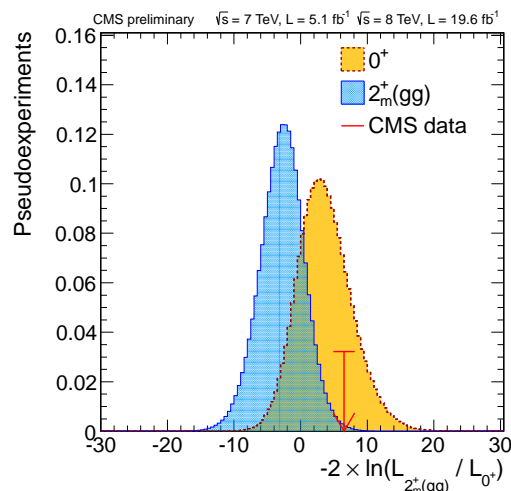
- Golden  $ZZH$  coupling as a benchmark ( $pp$  vs.  $H$ -factory vs. ILC)
  - mostly decay on LHC and production on  $e^+e^-$
  - kinematics:  $m(Z_i)$ ,  $\theta_i$ ,  $\Phi$  for spin=0; add  $\theta^*$  and  $\Phi_1$  for spin $\neq$ 0
  - $m(Z^*) \Leftrightarrow e^+e^-$  threshold scan
  - may combine with  $WWH$ , but cannot use  $e^+e^-WW \rightarrow \nu\bar{\nu}H$
  - no strict boundaries:  $Z(W)H$  and VBF contribute to LHC, ILC
  - fermion couplings discussed separately

# Path 1: Spin $> 0$

- Several test models adopted by LHC for  $ZZH$ ,  $WWH$ ,  $\gamma\gamma H$ ,  $ggH$

model	$X$ production	comments
$0^-$	any	pseudoscalar
$1^+$	$q\bar{q} \rightarrow X$	exotic pseudo-vector, not for $\gamma\gamma H$ , $ggH$
$1^-$	$q\bar{q} \rightarrow X$	exotic vector, not for $\gamma\gamma H$ , $ggH$
$2_m^+$	$q\bar{q} \rightarrow X$	graviton-like tensor with minimal couplings
$2_m^+$	$gg \rightarrow X$	graviton-like tensor with minimal couplings
$2_h^-$	$gg \rightarrow X$	“pseudo-tensor”

- Possible measure tensor structure, less motivated
  - for Snowmass may stick to a few **benchmark models** (e.g. above)



- LHC: MELA / BDT techniques, example:  
 CMS expect (observe)  $2_m^+$  vs SM  $0^+$ :  $1.9\sigma$  ( $2.7\sigma$ )  
 scales to 300/fb LHC  $\sim 10\sigma$

# Path 2: Mixture in $VVH$

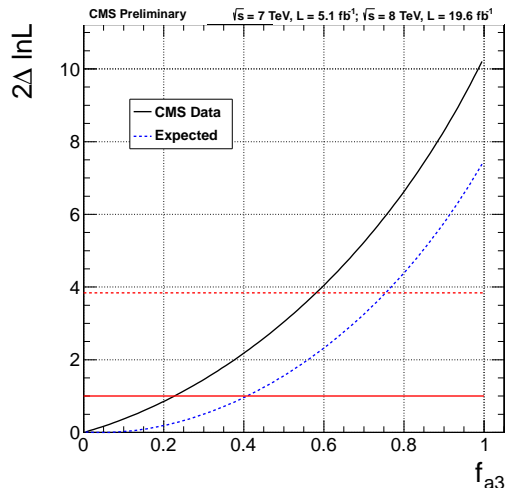
$ZZH$ ,  $WWH$  (SM  $g_1$ ),  $Z\gamma H$ ,  $\gamma\gamma H$ ,  $ggH$  (SM  $g_2$ ), or  $0^-$  ( $g_4$ )

$$A_{VV} \propto g_1 m_V^2 \epsilon_1^* \epsilon_2^* + g_2 f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + g_3 f_{\mu\alpha}^{*(1),\mu\nu} f_{\mu\alpha}^{*(2)} \frac{q_\nu q^\alpha}{\Lambda^2} + g_4 f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}$$

When  $g_1$  dominates,  $f_{g_4}$  is  $CP$ -violating fraction (here  $g_i = 1 \leftrightarrow \sigma_i$ ):

$$f_{CP} = f_{g_4} = \frac{|g_4|^2 \sigma_4}{|g_1|^2 \sigma_1 + |g_2|^2 \sigma_2 + |g_4|^2 \sigma_4}; \quad \phi_{g_4} = \arg\left(\frac{g_4}{g_1}\right)$$

$$f_{g_2} = \frac{|g_2|^2 \sigma_2}{|g_1|^2 \sigma_1 + |g_2|^2 \sigma_2 + |g_4|^2 \sigma_4}; \quad \phi_{g_2} = \arg\left(\frac{g_2}{g_1}\right)$$



- LHC: assuming SM and ignoring  $g_3$

CMS expect (observe)  $f_{CP} = 0.00 \pm 0.40$  ( $\pm 0.23$ )

scales to 300/fb LHC  $f_{CP} = 0.00 \pm 0.08$

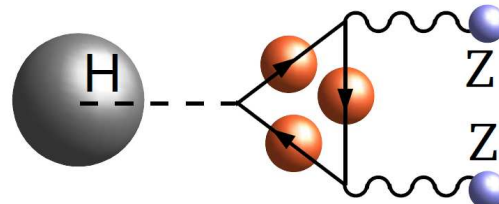
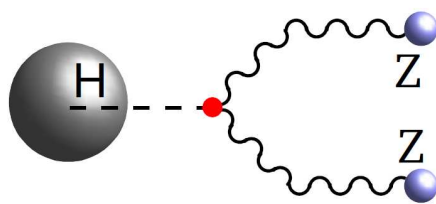
may include  $f_{g_2}$  in projections

# Mixture in $VVH$

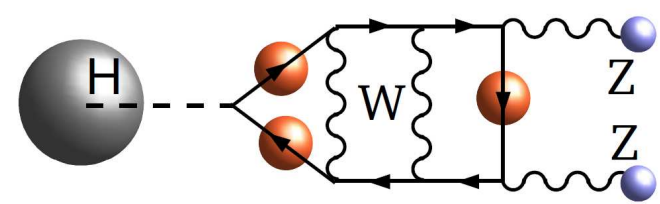
- Amplitude for  $X_{J=0} \rightarrow V_1 V_2$

$$A = v^{-1} \epsilon_1^{*\mu} \epsilon_2^{*\nu} \left( a_1 g_{\mu\nu} M_X^2 + a_2 q_\mu q_\nu + a_3 \epsilon_{\mu\nu\alpha\beta} q_1^\alpha q_2^\beta \right)$$

- SM Higgs  $0^+$ :  $(a_1)$   $CP$   $\sim \text{few}\%$   $(a_2)$   $CP$   $\sim 10^{-10}$  ?  $(a_3)$   $\cancel{CP}$



(or beyond SM)



(or beyond SM)

- 3 amplitudes (“experiment”)  $\Leftrightarrow$  3 coupling constants (“theory”)

$$A_{00} = -\frac{m_H^2}{v} \left( a_1 x + a_2 \frac{m_1 m_2}{m_H^2} (x^2 - 1) \right)$$

$$A_{\pm\pm} = +\frac{m_H^2}{v} \left( a_1 \pm i a_3 \frac{m_1 m_2}{m_H^2} \sqrt{x^2 - 1} \right)$$

$$x = \frac{m_H^2 - m_1^2 - m_2^2}{2m_1 m_2}$$

# Photon and Muon Colliders

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- Polarized beams on  $\mu^+\mu^-$  and  $\gamma\gamma$  colliders with  $s$ -channel production
  - would allow to measure  $A_{++}$  vs  $A_{--}$  amplitudes  $\Rightarrow$   $CP$  fraction
  - benchmark measurements  $f_{CP}$  in  $\mu^+\mu^-H$  and  $\gamma\gamma H$   
(not “easily” possible on LHC and  $e^+e^-$ )
- even if present,  $CP$  violation may be suppressed in  $ZZH$  coupling
  - if  $0^-$  coupling to  $ZZ$  (same for  $WW$ ) is suppressed  
 $ttH$ ,  $\tau\tau H$ ,  $Z\gamma H$  may have large  $CP$ -violation on LHC and  $e^+e^-$   
small- $f_{CP}$  & large-precision vs large- $f_{CP}$  & smaller-precision
  - $\mu^+\mu^-H$  and  $\gamma\gamma H$  would become key measurements on  $\mu\mu$  and  $\gamma\gamma$
- Feasibility study from  $\mu\mu$  and  $\gamma\gamma$  collider communities
  - need common convention for the quoted measurement



## Path 2: Mixture in $f\bar{f}H$

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- Mixture  $\tau^+\tau^-H, \mu^+\mu^-H, b\bar{b}H, t\bar{t}H$  harder to measure on  $e^+e^-$  &  $pp$ 
  - possible if polarization of fermion decay (production) is measured  
 $e^\pm$  beam polarization may help
  - feasibility in  $H \rightarrow \tau^+\tau^-$
  - feasibility in  $e^+e^-(pp) \rightarrow t\bar{t}H$
- Similar parameterization:

$$A_{f\bar{f}} \propto \frac{m_f}{v} \bar{u}_2 (\rho_1 + \rho_2 \gamma_5) v_1 = \frac{m_f}{v} \bar{u}_2 \rho (\cos \theta + e^{i\phi_{\rho_2}} \sin \theta \gamma_5) v_1$$

$$f_{CP} = f_{\rho_2} = \frac{|\rho_2|^2 \sigma_2}{|\rho_1|^2 \sigma_1 + |\rho_2|^2 \sigma_2} = \frac{1}{|\rho_1/\rho_2|^2 \sigma_1/\sigma_2 + 1} = \frac{1}{|\cot \theta|^2 \sigma_1/\sigma_2 + 1}$$

$$\phi_{\rho_2} = \arg \left( \frac{\rho_2}{\rho_1} \right)$$

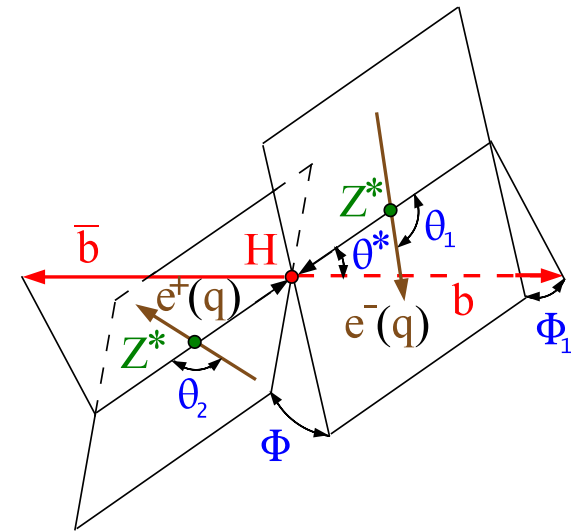
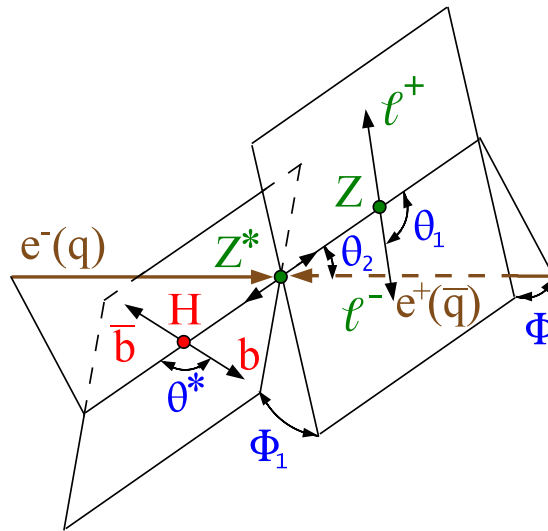
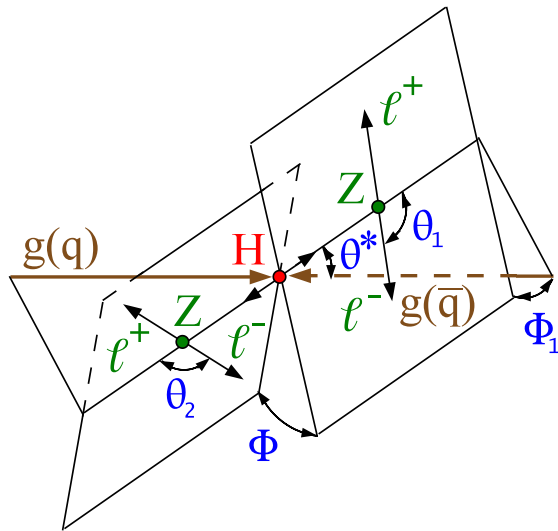
- deduce from fermion polarization:  $A_{\pm\pm} \propto (\rho_2 \pm \beta \rho_1)$

# Possible matrix for $pp$ vs. $H$ -factory vs. ILC

• LHC:  $gg \rightarrow H$

• H-factory:  $ee \rightarrow ZH$

• ILC:  $eeZZ \rightarrow eeH$



	LHC 300/fb	LHC 3000/fb	$e^+e^-$ 250 GeV	$e^+e^-$ 1 TeV
<b>spin-2</b> Grav. ...	$\sim 10\sigma$ ...	$\gg 10\sigma$ ...	? ...	? ...
$f_{CP}$ in $ZZH$	$\pm 0.08$	$\pm 0.03$ (?)	?	?
$f_{CP}$ in $\tau\tau H$	?	?	?	?
$f_{CP}$ in $ttH$	?	?	—	?
$f_{CP}$ in $Z\gamma H$	?	?	?	?

# Summary: Spin and Mixture for Snowmass-2013

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- We already know many things, but need to focus on projections:
  - $VVH$  ( $V = W, Z$ ) couplings at LHC reasonably well covered
  - $e^+e^-$  expectations and fermion couplings need to quantify better
  - quantify  $\mu^+\mu^- \rightarrow H$  and  $\gamma\gamma \rightarrow H$  feasibility of  $CP$  measurements

	LHC 300/fb	LHC 3000/fb	$e^+e^-$ 250 GeV	$e^+e^-$ 1 TeV	$\mu^+\mu^-$ 125 GeV	$\gamma\gamma$ 125 GeV
spin-2 Grav. ...	$\sim 10\sigma$ ...	$\gg 10\sigma$ ...	? ...	? ...	? ...	? ...
$f_{CP}$ in $VVH$	$\pm 0.08$	$\pm 0.03$ (?)	?	?	?	?
$f_{CP}$ in $\tau\tau H$	?	?	?	?	?	?
$f_{CP}$ in $ttH$	?	?	—	?	—	—
$f_{CP}$ in $\mu\mu H$	—	—	—	—	?	—
$f_{CP}$ in $\gamma\gamma H$	—	(?)	—	—	—	?

# ONE-SLIDE CONTRIBUTIONS

# ATLAS Snowmass Spin/CP studies

- Moriond results suggest the dominant spin-parity  $J^P=0^+$ : ATL-CONF-2013-013, ATL-CONF-2013-029, ATL-CONF-2013-031, CMS-CMS-PAS-HIG-13-002, CMS-PAS-HIG-13-003.
- Snowmass study: sensitivity to CP-mixing, anomalous couplings in  $H \rightarrow ZZ^{(*)} \rightarrow 4l$ .
  - As for the European strategy: generator level + smearing to accommodate for detector effects, event weights for trigger and lepton reconstruction efficiency.
$$A(X \rightarrow VV) \sim \underbrace{(a_1 M_X^2 g_{\mu\nu} + a_2 (q_1 + q_2)_\mu (q_1 + q_2)_\nu)}_{\text{CP-even}} + \underbrace{a_3 \epsilon_{\mu\nu\alpha\beta} q_1^\alpha q_2^\beta}_{\text{CP-odd}} \epsilon_1^{*\mu} \epsilon_2^{*\nu}$$
- Available Monte Carlo generators:
  - JHU (LO): allows to vary  $a_1, a_2, a_3$  independently.
  - MadGraph 5 + aMC@NLO: introduces a single mixing angle between the 1<sup>st</sup> and the 3<sup>d</sup> components of the amplitude.
- Monte Carlo re-weighting: available in JHU (ratio of  $|M|^2$ ); can be introduced in MG5 and aMC@NLO (pre-defined set of weights corresponding to different mixing).
- Observables: it is probably most interesting to estimate the sensitivity to the mixing angle between 1<sup>st</sup> and the 3<sup>d</sup> components and possibly to the phase.  $f_{a3}$ ?
- Study methods: Matrix element likelihood fit with free parameters, Modeling mixing strength by re-weighting and comparing with  $J^P=0^+$ , Optimal observables analysis, Angular asymmetries.
- Given there is enough taskforce, we can add study of the VBF forward jets and fermionic channels:  $H \rightarrow \tau\tau/\mu\mu$ .

# Spin-CP studies of the new boson for Snowmass

**Study kinematic distributions of  $X \rightarrow VV \rightarrow 4$  fermions to extract tensor amplitude structure of production and decay of the new boson.**

using JHU generator and MELA method:

- <http://www.pha.jhu.edu/spin/>
- Phys. Rev. D 81, 075022 (2010)
- Phys. Rev. D 86, 095031 (2012)

Evaluate the sensitivity at future pp and (possibly) e+e- colliders for:

(gen-level studies with smearing+acceptance cuts)

## □ CP mixing studies assuming spin 0

$$A(X_{J=0} \rightarrow V_1 V_2) = v^{-1} \left( g_1 m_V^2 \epsilon_1^* \epsilon_2^* + g_2 f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + g_4 f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu} \right)$$

with present LHC statistics pure 0- ruled out ( $g_i=0$  for  $i \neq 4$ ) -> next steps

- test **mixed hypotheses** with more than one  $g_i \neq 0$  (with interference included)
- **fit directly the fractions and phases of  $g_i$**  from kinematic distributions

Eg: 0.08 precision expected on  $g_4$  fraction with  $300 \text{ fb}^{-1}$  at LHC

## □ Exotic spin scenarios (similar, more complex, formula as above available in cited papers for spin>0)

most basic (minimal couplings) scenarios under test at LHC -> next steps

- test wide range of **scenarios** (identify the ones **with kinematics very similar to 0+ SM case**)
- more model independent approach: **production-independent spin tests**  
**mixing-independent spin tests**

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*Main contributors: S.Bolognesi<sup>1</sup>, Y.Gao<sup>2</sup>, N.Tran<sup>2</sup>, A.Whitbeck<sup>1</sup> (1= Johns Hopkins, 2=FNAL)*

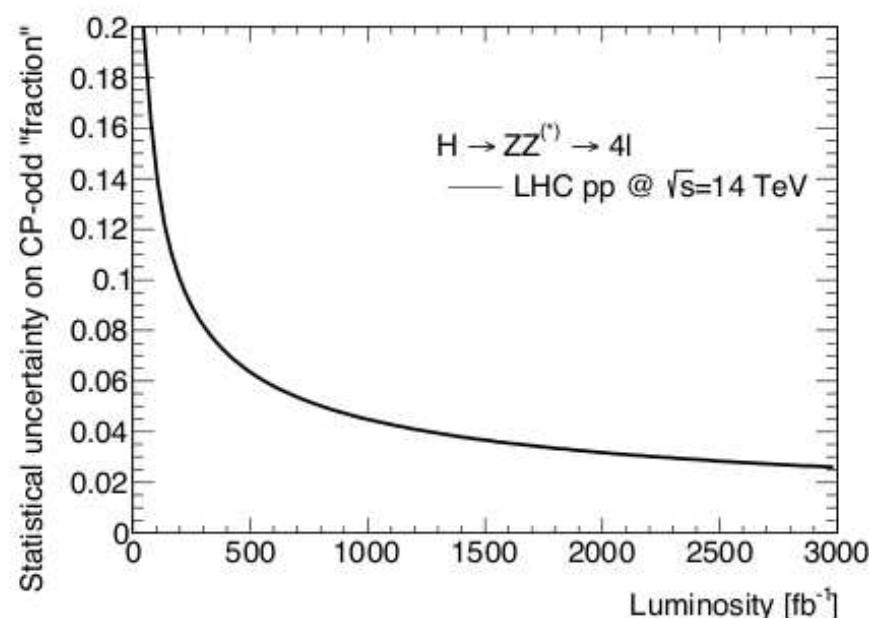


## E. Feng (ANL): Higgs CP Fraction

- Matrix element method to measure spin, CP, and couplings in  $H \rightarrow ZZ \rightarrow 4l$ 
  - Unbinned maximum likelihood fit to analytical prediction using 3 masses ( $m_{4l}, m_{12}, m_{34}$ ) and 5 angles ( $\cos(\theta^*), \phi_1, \cos(\theta_1), \cos(\theta_2), \Delta\phi$ ) from 4 leptons
- Characterize sensitivity to CP-odd fraction projected onto  $H \rightarrow ZZ$  final state by fitting to linear combination of  $0^+$  and  $0^-$  hypotheses as function of 14 TeV lumi
- CP-odd component corresponds to non-zero  $g_4^{(0)}$  form factor in ME:

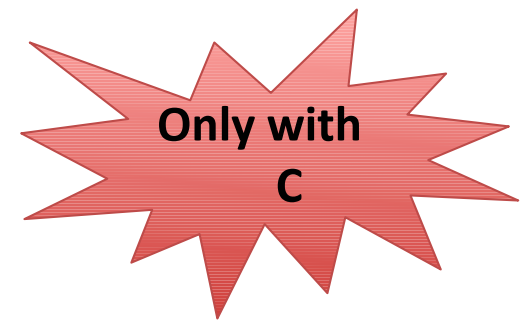
$$A(X \rightarrow V_1 V_2) = v^{-1} \left( g_1^{(0)} m_V^2 \epsilon_1^* \epsilon_2^* + g_2^{(0)} f_{\mu\nu}^{*(1)} f_{\mu\nu}^{*(2)} + g_3^{(0)} f_{\mu\nu}^{*(1)} f_{\mu\alpha}^{*(2)} \frac{q_\nu q^\alpha}{\Lambda^2} + g_4^{(0)} f_{\mu\nu}^{*(1)} \tilde{f}_{\mu\nu}^{*(2)} \right),$$

- Statistical uncertainty of  $\sim 8\%$  (3%) can be achieved with 300 (3000)  $\text{fb}^{-1}$  at 14 TeV
  - Includes detector acceptance
  - Generating fastsim for systematics, which should be relatively small
- Additional studies may include non-minimal couplings for spin-2, but lower sensitivity



$\zeta_2$  is the degree of circular polarization  
 $(\zeta_3, \zeta_1)$  are the degrees of linear polarization

In s-channel production of Higgs:



$$|\overline{\mathcal{M}^{H_i}}|^2 = |\overline{\mathcal{M}^{H_i}}|_0^2 \left\{ [1 + \zeta_2 \bar{\zeta}_2] + \mathcal{A}_1 [\zeta_2 + \bar{\zeta}_2] + \mathcal{A}_2 [\zeta_1 \bar{\zeta}_3 + \zeta_3 \bar{\zeta}_1] - \mathcal{A}_3 [\zeta_1 \bar{\zeta}_1 - \zeta_3 \bar{\zeta}_3] \right\}$$

== 0 if CP is conserved

== +1 (-1) for CP is conserved for  
 A CP-Even (CP-Odd) Higgs

➡ If  $\mathcal{A}_1 \neq 0$ ,  $\mathcal{A}_2 \neq 0$  and/or  $|\mathcal{A}_3| < 1$ , the Higgs  
 is a mixture of CP-Even and CP-Odd states

➡ Possible to search for CP violation in  
 $\check{\chi} \check{H} \check{\chi}$  fermions without having to measure their polarization

➡ In bb, a  $\leq 1\%$  asymmetry can be measure with 100 fb<sup>-1</sup>  
 that is, in 1/2 years

arXiv:0705.1089v2